
Instructions: Write complete legible solutions to the following problems in the space provided. Be sure to supply all the necessary steps that lead to your answers.

1. Let $S = \{(1, -2, 1), (1, 1, 2), (3, -3, 4)\}$, determine which of the following vectors is a member of $\text{Span}(S)$.

a. $(1, -8, -1)$

b. $(5, 1, 8)$

c. $(1, 2, 1)$

- b. For those in part that are in the $\text{Span}(S)$, give their coordinate vector relative to S .

2. Determine if the set of vectors are linear independent

a. $1, \sin x, \sin 2x$

b. $\mathbf{p}_1 = 2 + 2x + 2x^2, \mathbf{p}_2 = 3x^2, \mathbf{p}_3 = x + x^2,$

3. Find the coordinate vector of \mathbf{P} relative to the set $S = \{\mathbf{P}_1, \mathbf{P}_2, \mathbf{P}_3\}$, then write \mathbf{P} as linear combination of members of S , where

$$\mathbf{P}_1 = 2 + x + 4x^2, \mathbf{P}_2 = 1 - x + 3x^2, \mathbf{P}_3 = 3 + 2x + 5x^2, \text{ and } \mathbf{P} = 6 + 11x + 6x^2$$

4. Find the dimension of $\text{span}(S)$, where

$$S = \{(1,1,1,1), (0,1,1,1), (1,1,1,0), (1,0,0,0), (0,0,0,1)\}$$

5. Determine if the given set S is linear independent. Then find a basis for the space spanned by the linearly independent subset of S , and express any extra matrices as a linear combination of the basis.

$$S = \left\{ \begin{bmatrix} 1 & 1 \\ 2 & 1 \end{bmatrix}, \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 3 \\ 5 & 1 \end{bmatrix} \right\}$$