

Give complete solutions to the following problems be sure to provide all the necessary steps to support your answers.

1. Let  $\mathbf{W}$  be the plane in  $\mathbb{R}^3$  with equation  $x + 2y - z = 2$ , find a parametric equation for  $\mathbf{W}^\perp$
  
2. Let  $S = \{(1, 1, 2, 1), (1, -1, 1, 1), (1, 3, 3, 1)\}$  be a subset of  $\mathbb{R}^4$  with the Euclidean inner product, find the orthogonal complement of  $S$ .
  
3. Let  $\mathbb{R}^2$  have the Euclidean inner product. Use the Gram-Schmidt process to transform the set  $S$  into an orthonormal basis for. Draw both the set  $S$  and the ON basis on the  $xy$ -plane.  
$$S = \{(-2, 1), (2, 1)\}$$

Problems 4, 5 and 6.

Let  $S = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\} = \{(0,1,0), (1,1,1), (0,1,1)\}$

4.
  - a) Show that S forms a basis for  $\mathbb{R}^3$ .
  - b) Transform S into an orthonormal basis for  $\mathbb{R}^3$ .
  - c) Express  $\mathbf{v} = (2, -1, 1)$  as a linear combination of the ON basis from part b

5. Find an orthonormal basis for  $\text{Span}(S)$  for the set S in problem 2, then find the projection of  $\mathbf{v} = (3, 1, 2, 1)$  onto  $\text{Span}(S)$ .

6. Let  $A = [\mathbf{v}_1 \quad \mathbf{v}_2 \quad \mathbf{v}_3]$ , find matrices Q and R such that  $A = QR$